

**First Semester M.TECH (Mathematics Engineering)**

**Examination Aug/Sep-2015**

**Numerical Analysis**

**Time:-3Hours**

**Max. Marks: -80**

**Section-A**

**Answer any five questions:**

**(6\*5)**

- Q1. Find the value of  $\int_0^1 \frac{x^2}{1+x^3} dx$ , using Simpson's 1/3 rule by Dividing the range into four equal parts. Also find the error.
- Q2. Represent the function  $f(x) = x^4 - 12x^3 + 24x^2 - 30x + 9$  and its successive differences into factorial notation.
- Q3. Show that  $Y_{k+2} - 4Y_{k+1} + 4Y_k = 0 \dots (i)[K= 0,1]$  has the solution.
- Q4. Write down the Lag range's Interpolation formula for unequal intervals.
- Q5. Use Stirling's formula to find  $Y_{28}$  given:  
 $Y_{20} = 49225, Y_{25} = 48316, Y_{30} = 47236, Y_{35} = 45926, Y_{40} = 44306$
- Q6. Show that  $\int_0^1 \frac{dx}{1+x} = \log 2 = 0.69315$
- Q7. Given  $Y_{20} = 24, Y_{24} = 32, Y_{28} = 35, Y_{32} = 40$ . Find  $y_{25}$  by Bessel formula.
- Q8. Evaluate  $\int_0^4 e^x dx$ , by Simpson's rule, using the data  $e = 2.72, e^2 = 7.59, e^3 = 20.09, e^4 = 54.60$  and compare it with the actual value.

**Section- B**

**Answer any two questions:**

**(10×2)**

- Q11 Solve the following system of equation by
- Gauss seidal Iteration method.
  - Jacobi Iterative method.
- $$27x + 6y - z = 85,$$
- $$bx + 15y - 2z = 72,$$
- $$x + y + 54z = 110.$$

**Section- C**

**Answer any two questions:**

**(15×2)**

Q12. Let  $A = \begin{pmatrix} 3 & 12 & 9 \\ 2 & 10 & 12 \\ 1 & 12 & 2 \end{pmatrix}$  then find two triangular

Matrices: L (lower triangular) and U (upper triangular) such that  $A = LU$ , using the diagonal elements of  $L$  as 3, 1, 5. Hence obtain  $A^{-1}$

Q13. Solve by relaxation method the Laplace equation  $\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} = 0$ . Inside the square bounded by lines  $x = 0$ ,  $x = 4$ ,  $y = 0$ ,  $y = 4$ , given that  $u = x^2 y^2$  on the boundary.

Q14. Explain in detail the solution of elliptic equations by Relaxation method. Also write its working methods.